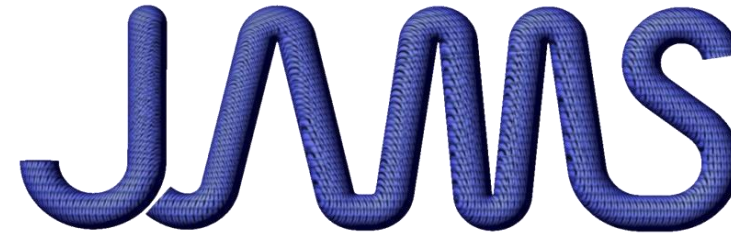




**CMH-17**  
COMPOSITE MATERIALS HANDBOOK



JOINT ADVANCED MATERIALS & STRUCTURES  
CENTER OF EXCELLENCE

# An Engineering Approach for Damage Growth Analysis of Sandwich Structures Subjected to Combined Compression and Pressure Loading

Waruna Seneviratne, John Tomblin, Shenal Perera  
Pirashandan Varatharaj, Vishnu Saseendran

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May 22-23, 2019



WICHITA STATE  
UNIVERSITY

NATIONAL INSTITUTE  
FOR AVIATION RESEARCH



# Research Team

- **National Institute for Aviation Research**

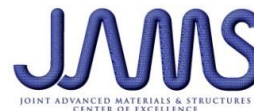
- PI: Waruna Seneviratne, PhD
- PI: John Tomblin, PhD
- Shenal Perera
- Pirashandan Varatharaj
- Vishnu Saseendran, PhD

- **FAA**

- Zhi-Ming Chen, PhD (Current TM)
- Larry Ilcewicz, PhD



Kansas Aviation Research & Technology Growth Initiative





# An Engineering Approach for Damage Growth Analysis of Sandwich Structures Subjected to Combined Compression and Pressure Loading

## • Motivation and Key Issues

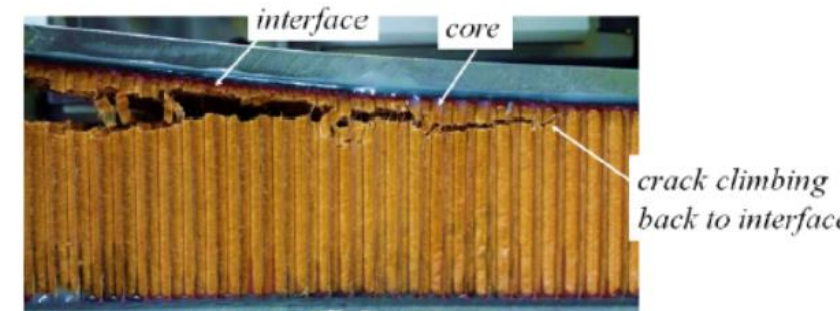
- Thermo-mechanical loads during ground-air-ground (GAG) cycling result in localized mode I stresses that cause further delamination/disbond/core fracture growth.

## • Objective

- Develop an engineering approach for damage tolerance analysis of sandwich structures subjected to combined mechanical and pressure loads.

## • Approach [Shown in the next slide]

- Engineering Approach [Discussed in next slide]
  - SCB Testing (Obtain  $G_{IC}$  fracture toughness values )
  - FEA Analysis on SCB Test and Validate modeling techniques
  - Develop a test method for GAG (Edgewise Compression) specimens.
  - Develop High Fidelity FEA models for GAG Specimens
  - Blind Predictions Comparing GAG FEA Data with Test Data

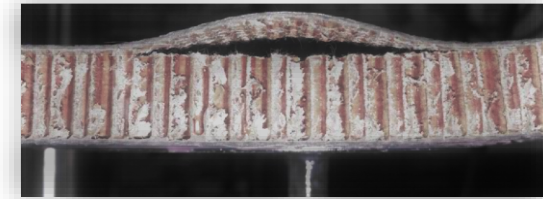




# Accomplishments

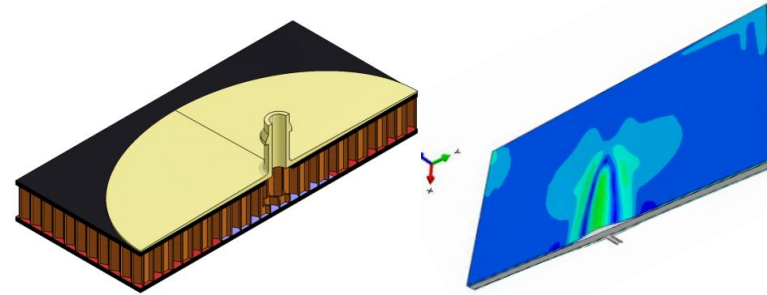
## ★ Mode I ( $G_{Ic}$ ) Fracture Toughness of Composite Sandwich Structures for Use in Damage Tolerance Design and Analysis

- Volume 1: *Static Testing Including Effects of Fluid Ingression* (DOT/FAA/TC-16/23)
- Volume 2: *Fatigue Testing Including Effects of Fluid Ingression* (DOT/FAA/TC-17/06)
- Volume 3: *Damage Growth in Sandwich Structures* (DOT/FAA/TC-17/7)
- Volume 4: *Investigation of Face/Core Interface Debonding in Aircraft Sandwich Composites Subjected to Combined Pressure and In-plane Loading: An Engineering Approach* (On Going)



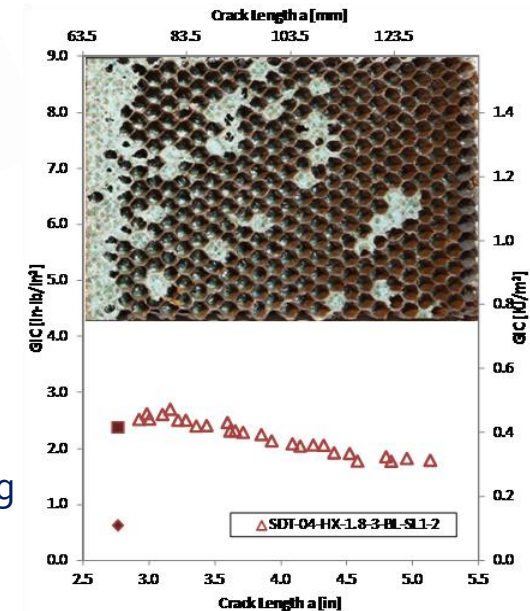
## ★ Other Contributions to ASTM D30 & CMH-17

- CMH-17 Rev. H chapters/sections (*completed review*)
- SCB Fracture test standard development ASTM D30



## ★ Other Publications

- Damage Initiation and Fracture Analysis of Honeycomb Core Single Cantilever Beam (SCB) Sandwich Specimen (*submitted to JSSM*)
- Damage Growth Analysis of Sandwich Structures Subjected to Combined Compression and Pressure Loading (*Accepted for ASC 34<sup>th</sup> Technical Conference*)

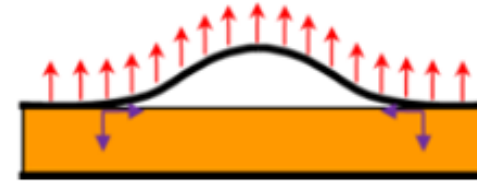




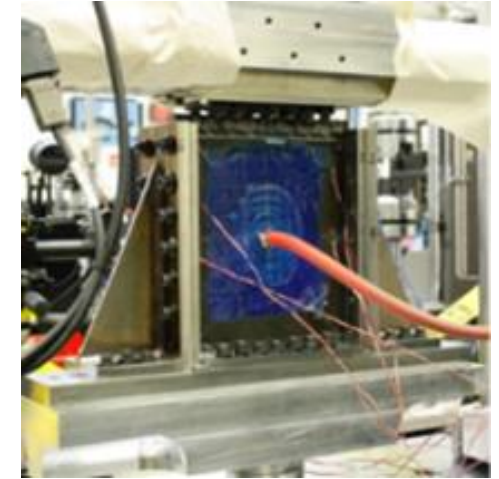


# Analysis – Engineering Approach

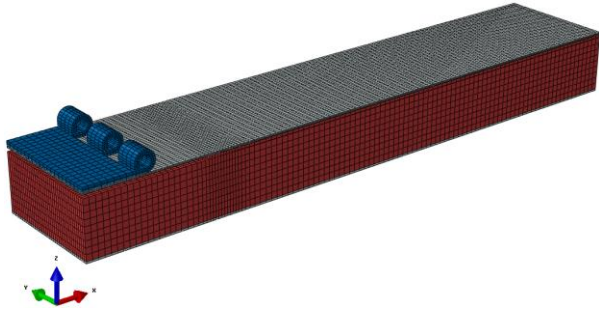
- SCB → GAG



## GAG Experimental Setup



## SCB FE Model



Structural Configuration(s)

SCB (Experiments)

Calibration I

SCB (FEM Approach)

Verification

SCB (Closed-Form Solutions)

SCB (Parametric Study)

Validation I

SCB (Additional Experiments)

- ✓ Guidelines for SCB analysis and testing
- ✓ Identify limitations
- ✓ Recommended practices for analysis and testing

GAG (FEM Approach)

Calibration II

GAG (Experiments)

- ✓ Guidelines for GAG analysis and testing
- ✓ Identify scaling issues
- ✓ Identify limitations
- ✓ Recommended practices for analysis and testing

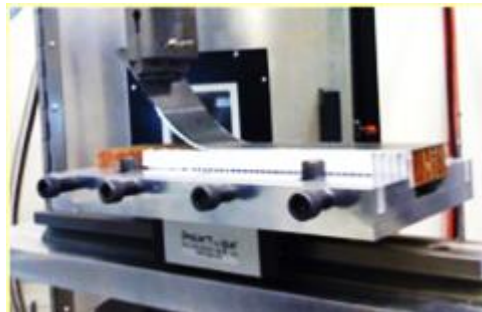
GAG (Parametric Study)

Validation II

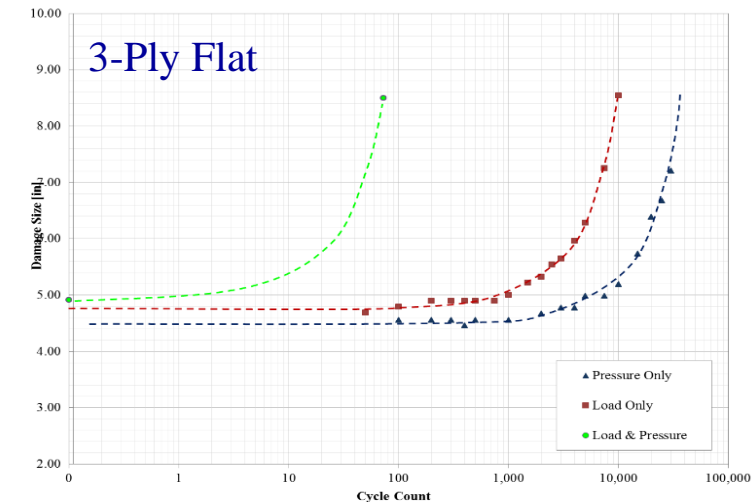
GAG (Additional Experiments)

Critical Damage Envelop/Threshold

## SCB Experimental Setup



## GAG Loading Cycles





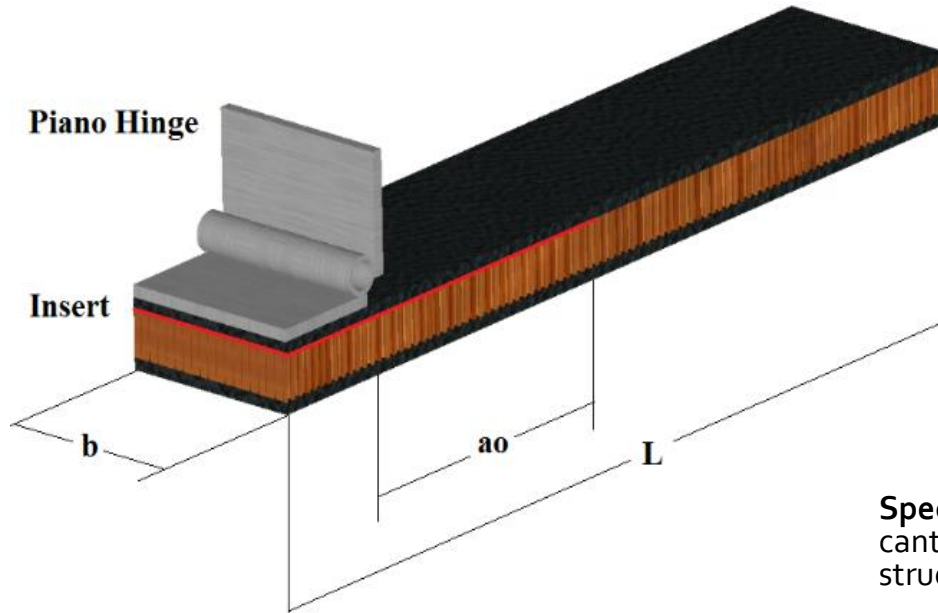
# Outline

- **SCB Test Configuration**
  - **Materials & Test Setup (translatable base)**
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  - Comparison of Analytical, FEA & Exp. Results
- Finite Element Model Description of SCB Specimens
  - Cohesive-based modeling approach
- GAG - Edgewise Compression (EWC) Test Configuration w/t Pressure Loading
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- Summary & Future Work



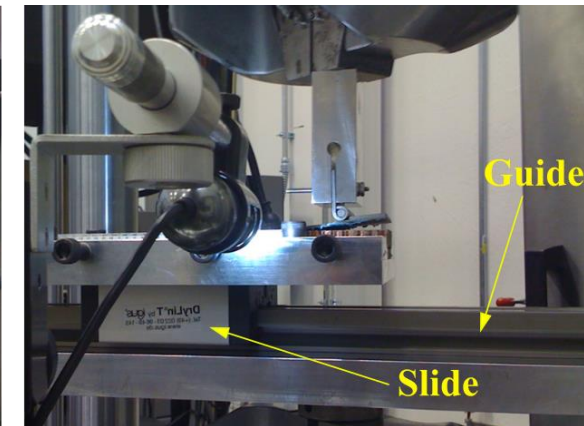
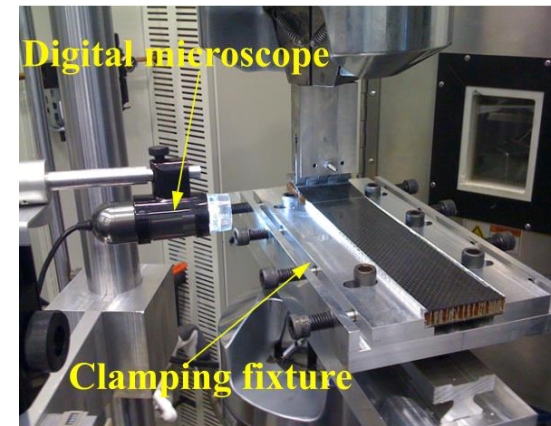
# SCB Test Configuration

- **Materials**
  - Facesheet: T650 – 5320 PW
  - Core: Hexcel HRH-10
  - Adhesive: FM300 - 2
- **Dimensions**
  - $L = 254\text{mm}$
  - $b = 50.8\text{mm}$
- **Piano Hinge**
  - Bonded using EA9394
- **Prescribed Crack**
  - Teflon® inserts
  - $a_o = 50.8\text{mm}$



## Test Matrix

Case	Facesheet Material	Ply	Cell Size (mm)	Core Density (kg/m <sup>3</sup> )	Core Thickness (mm)
1	T650/5320-PW	4	3.2	48.0	25.4
2	T650/5320-PW	4	3.2	96.0	12.7
3	T650/5320-PW	4	9.5	48.0	12.7
4	T650/5320-PW	8	3.2	96.0	12.7



Specimen sizing conforms w/t: Ratcliffe, James G., and James R. Reeder. "Sizing a single cantilever beam specimen for characterizing facesheet–core debonding in sandwich structure." *Journal of Composite Materials* 45.25 (2011): 2669-2684.



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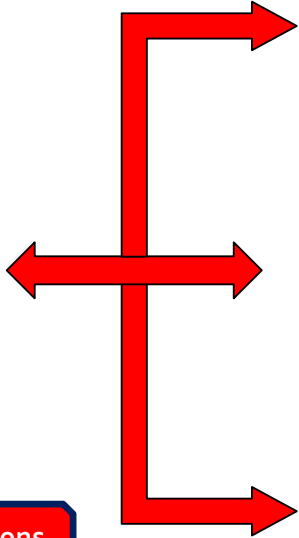




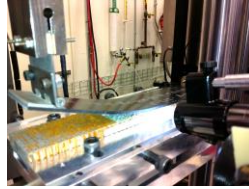
# Foundation Model Approach & Validation

## Python Based Suite

Python Suite



**SCB Fracture Tests**  
Compliance,  $C = \delta/P$   
crack length,  $a$

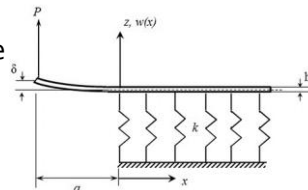


**SCB FE-Model**  
Compliance & energy-release rate validation



Core properties:  
*Gibson-Ashby model*

**Foundation model**  
Compliance & energy-release rate validation



**Winkler-based foundation model**

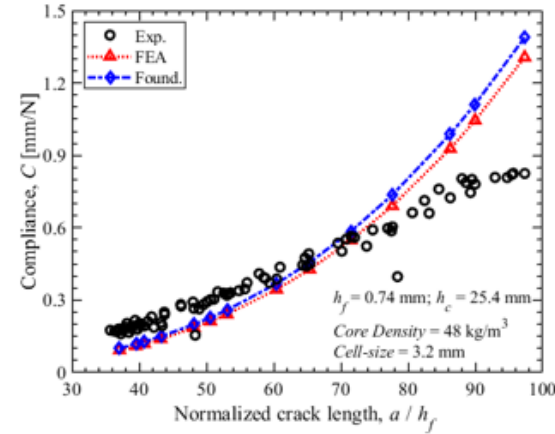
Closed – Form Expressions

$$C = \frac{\delta(x = -a)}{P} = \frac{4\lambda}{k} \left[ \frac{\lambda^3 a^3}{3} + \lambda^2 a^2 + \lambda a + \frac{1}{2} \right]$$

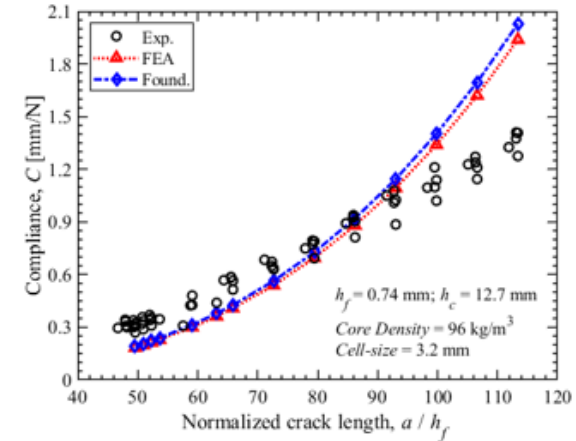
$$G = \frac{2P^2 \lambda^2}{bk} \left[ \lambda^2 a^2 + 2\lambda a + 1 \right]$$

$$\lambda = \sqrt[4]{\frac{k}{4E_f I}} \quad k = \frac{E_c b}{h_c / 4}$$

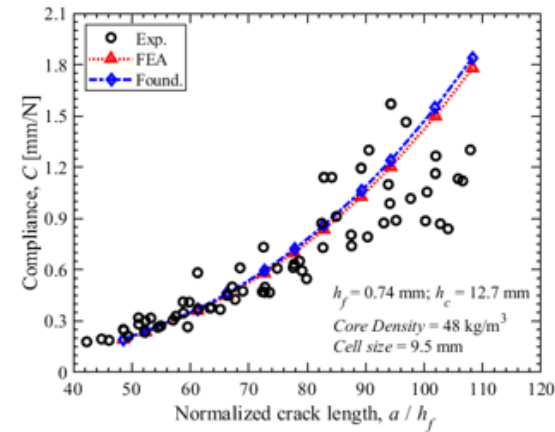
## Compliance vs. crack length



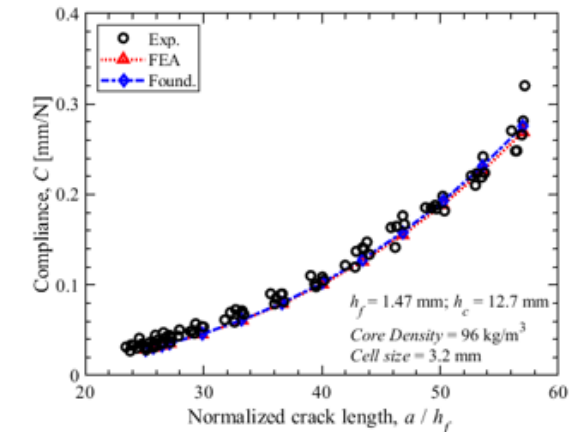
(a)



(b)



(c)



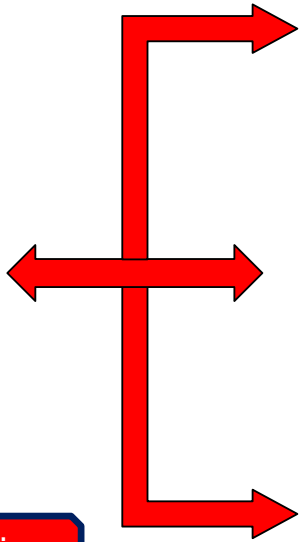
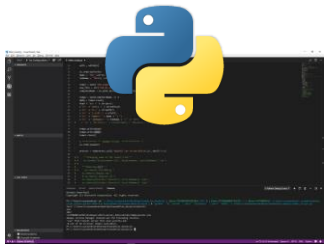
(d)



# Foundation Model Approach & Validation

## Python Based Suite

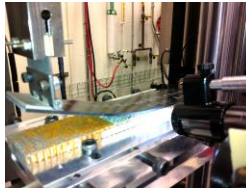
Python Suite



### SCB Fracture Tests

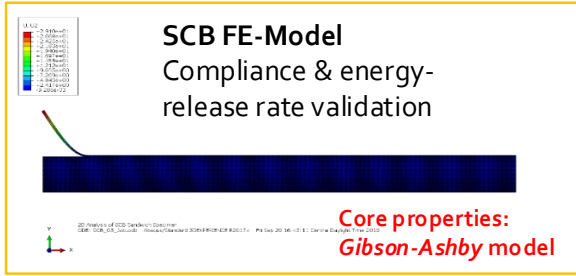
Compliance,  $C = \delta/P$   
crack length,  $a$

Initiation fracture toughness:  
*Modified Beam Theory (MBT)*



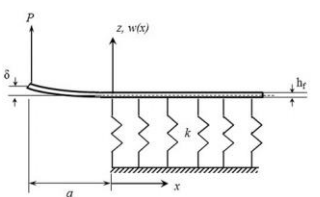
### SCB FE-Model

Compliance & energy-  
release rate validation



### Foundation model

Compliance &  
energy-release rate  
validation



**Winkler-based  
foundation model**

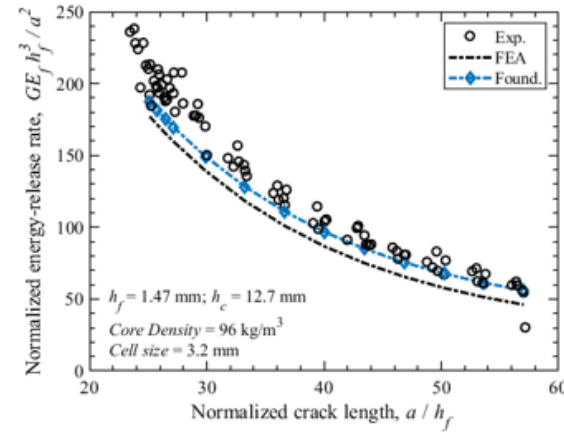
Closed – Form Expressions

$$C = \frac{\delta(x = -a)}{P} = \frac{4\lambda}{k} \left[ \frac{\lambda^3 a^3}{3} + \lambda^2 a^2 + \lambda a + \frac{1}{2} \right]$$

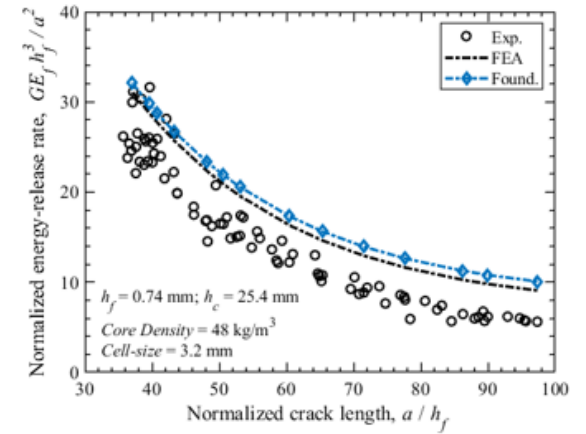
$$G = \frac{2P^2 \lambda^2}{bk} \left[ \lambda^2 a^2 + 2\lambda a + 1 \right]$$

$$\lambda = \sqrt[4]{\frac{k}{4E_f I}} \quad k = \frac{E_c b}{h_c / 4}$$

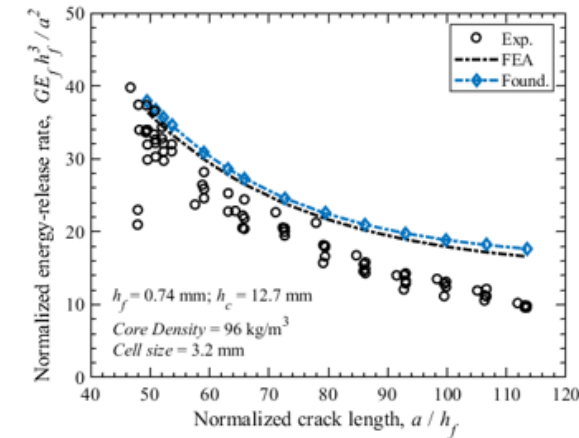
## Energy-release rate vs. crack length



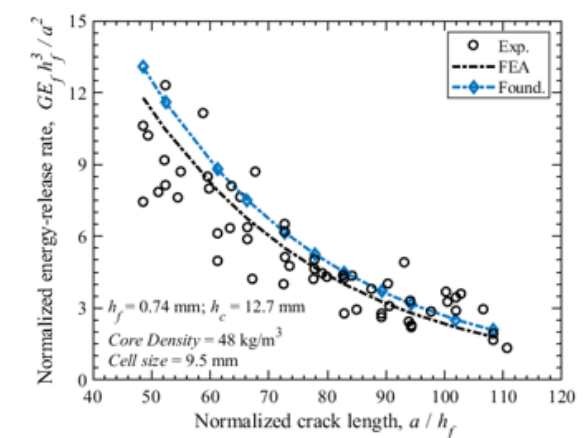
(a)



(b)



(c)



(d)



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# FEA – SCB Model Description and Approach

El-Sayed, S., & Sridharan, S. (2002). Cohesive layer models for predicting delamination growth and crack kinking in sandwich structures. *International Journal of Fracture*, 117(1), 63-84.

- **Cohesive zone** to model the damage in the core.
- Four configurations considered:
  - Core density (48 96 kg/m<sup>3</sup>) & Thickness (12.7, 25.4 mm)
  - Cell size (3.2, 9.5 mm)
  - Face-sheet thicknesses (4, 8-ply)
- Failure modeled in core using cohesive elements (located beneath meniscus layer)

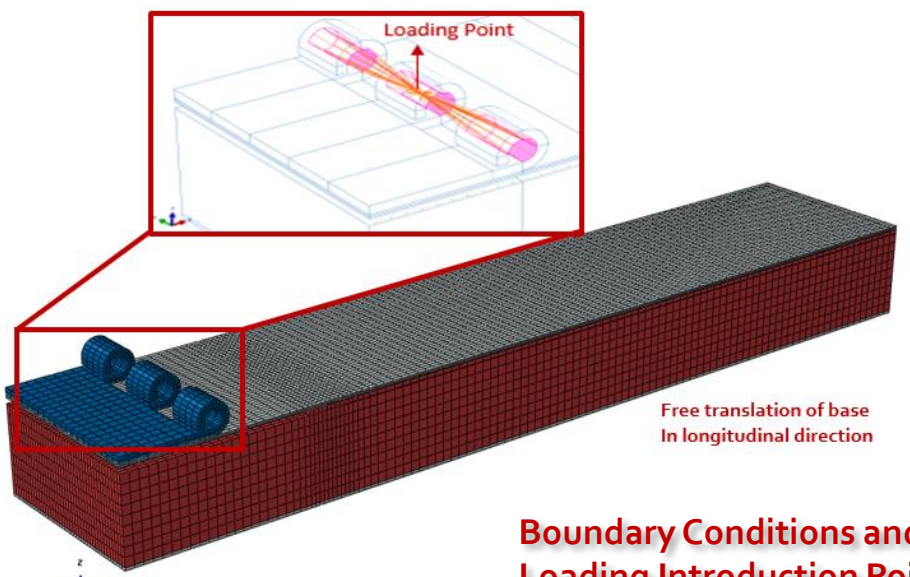
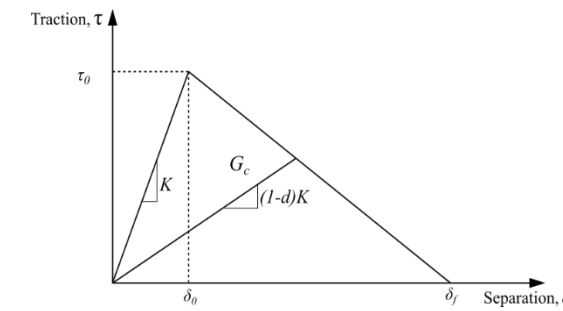


**G<sub>1c</sub>** →

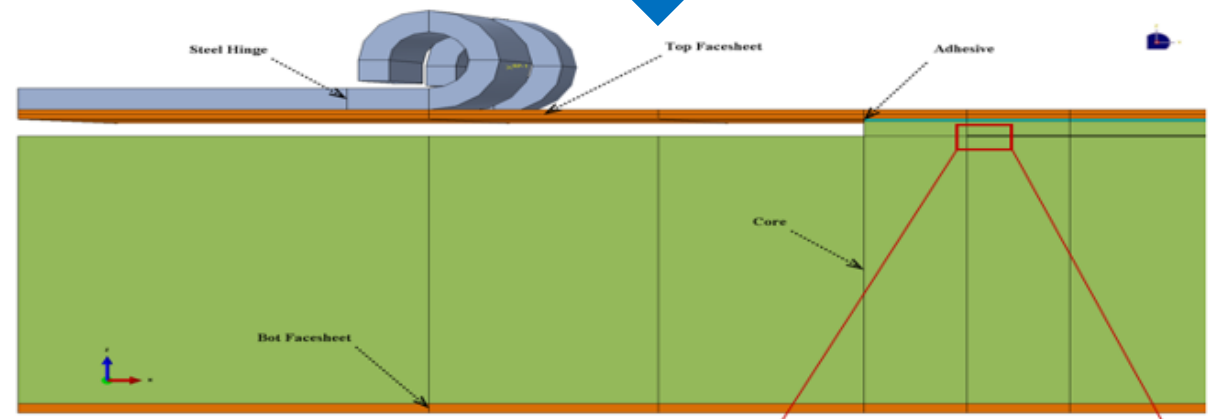
$$\tau_0 = \frac{4}{27} \sqrt{\frac{12E_c G_{1c}}{h_{eff}}} \quad K_n = \frac{E_c}{h_{eff}}$$



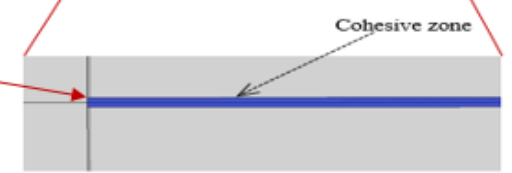
Core - Homogenous medium  
(Gibson-Ashby Approach)



**Boundary Conditions and Loading Introduction Point**



**Damage in the core**

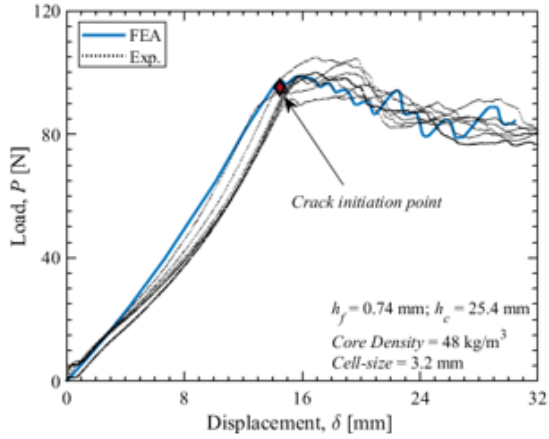




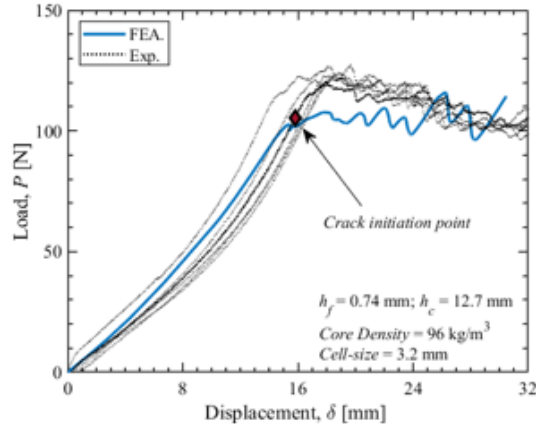


# Comparison of FE & Exp. Results

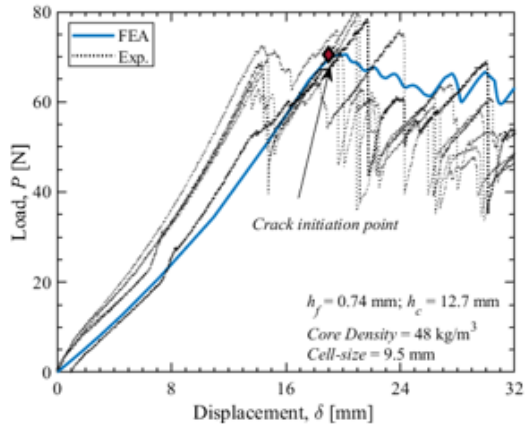
## Critical Load and Displacement Comparison



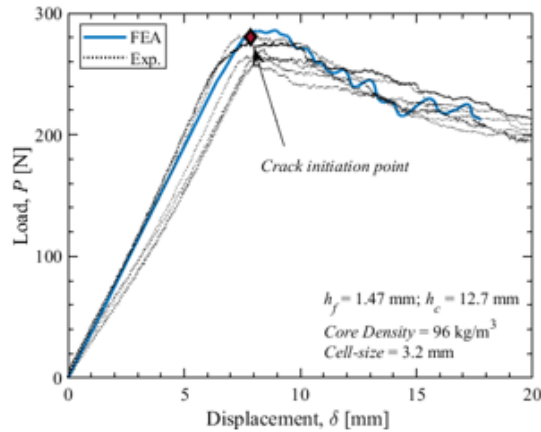
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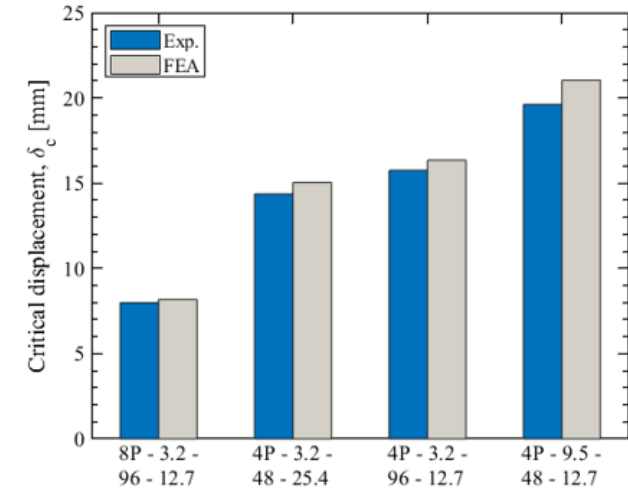
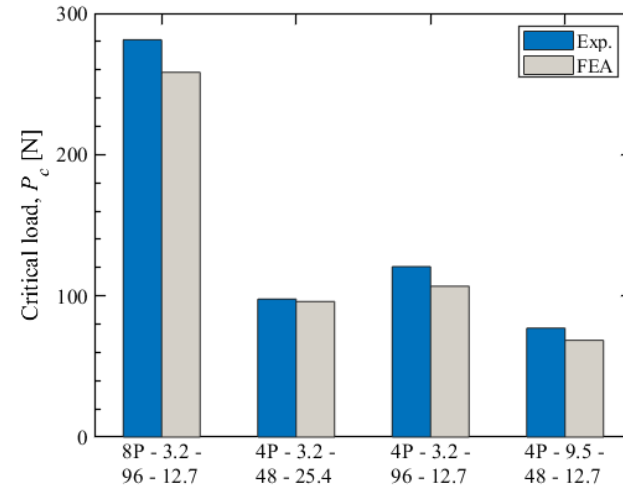
(b)



(c)



(d)



Case	Facesheet Material	Plies	Cell Size (mm)	Core Density (kg/m <sup>3</sup> )	Core Thickness (mm)	Exp. Load (N)	Predicted Crack Initiation Load	
							FEA Load (N)	Error (%)
1	T650/5320-PW	4	3.2	48.0	25.4	97.7	96.0	-1.8
2	T650/5320-PW	4	3.2	96.0	12.7	120.7	106.8	-11.5
3	T650/5320-PW	4	9.5	48.0	12.7	77.2	68.5	-11.3
4	T650/5320-PW	8	3.2	96.0	12.7	258.2	281.3	8.9

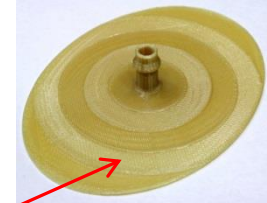
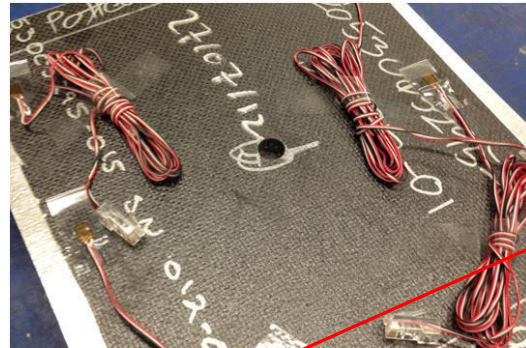
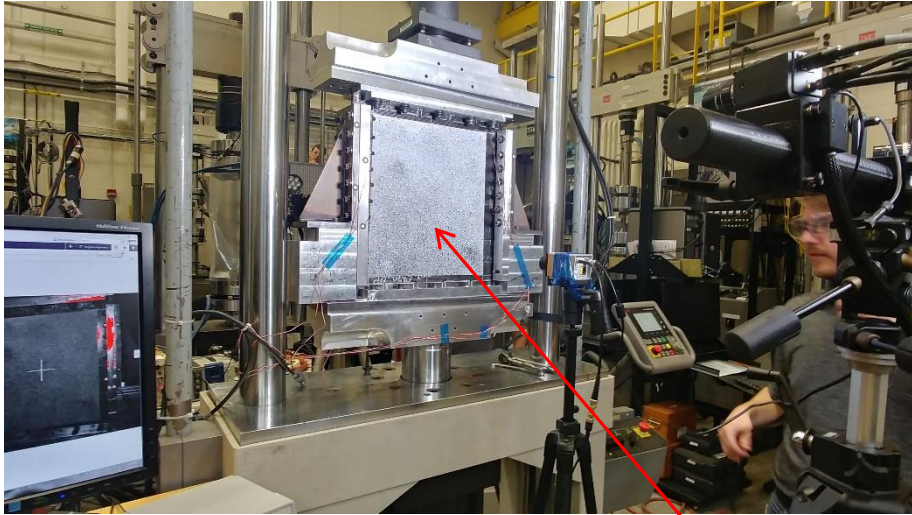


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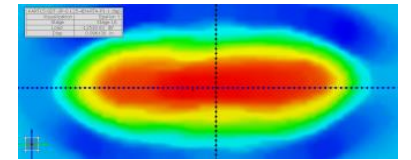
# GAG - Edgewise Compression (EWC) Test Setup



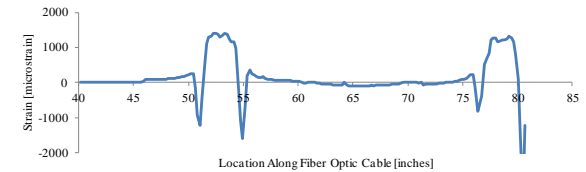
Hysol EA9309.3NA Epoxy

3D printed (Ultem) pressure port

## Damage Growth monitoring

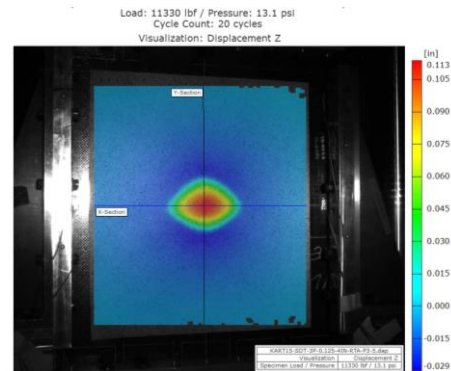
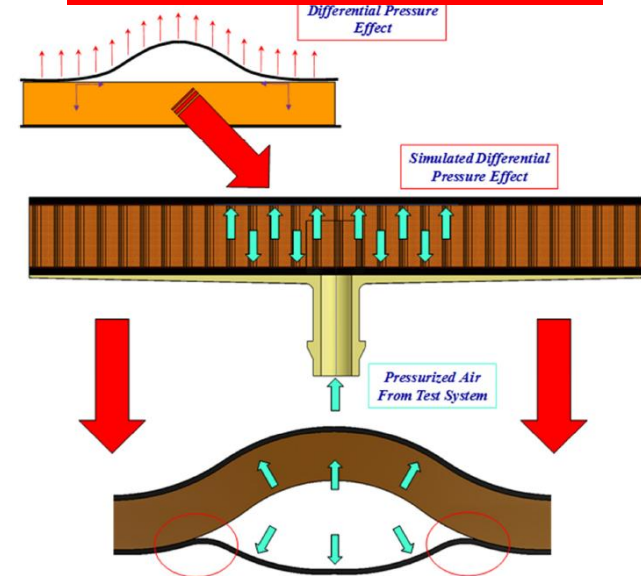


Digital Image Correlation (DIC)



Distributed fiber optic strain sensors

## Pressure Simulation



DIC speckle pattern on front and back sides

Ability to accommodate various specimen sizes  
• 10x12 (shown) and 18x20 (test size)

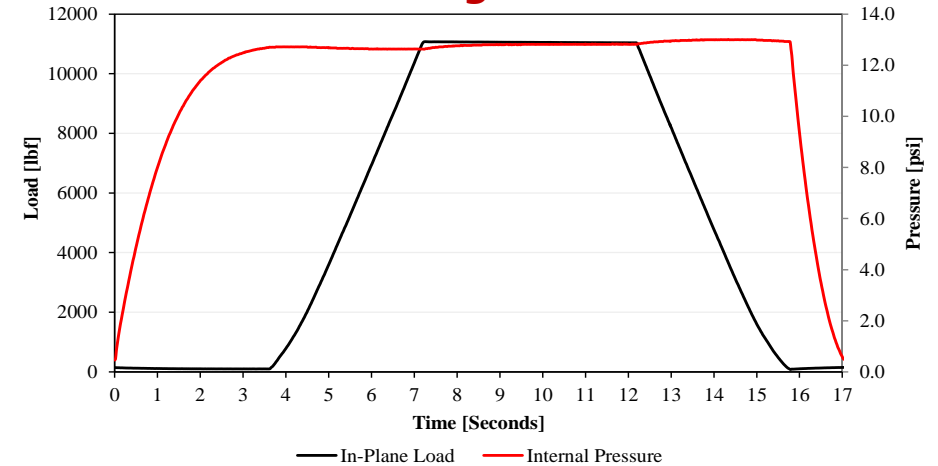




# GAG (EWC) Quasi Static Testing w/t Pressure Loading

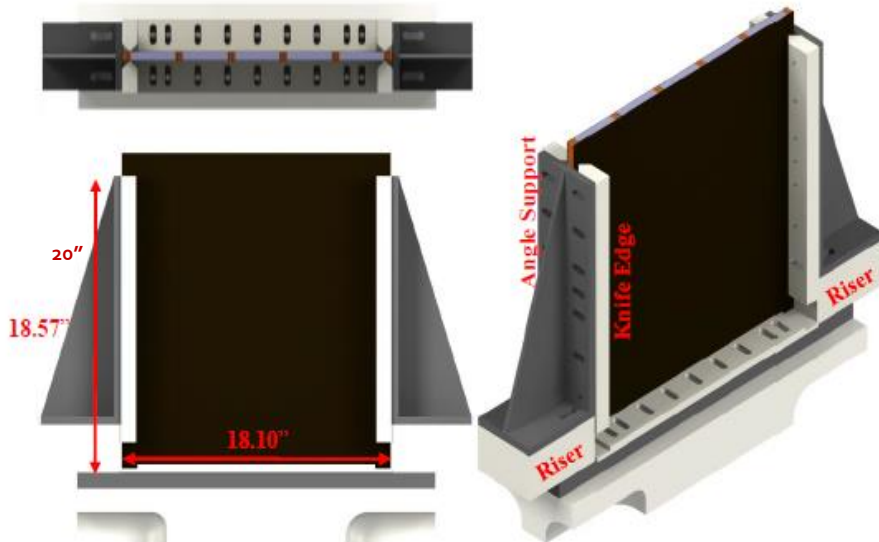
- Test rig developed for combined compression (in-plane) & pressure loading
- Face sheet & core parameters altered
- Ability to accommodate various specimen sizes

**Loading Condition**



**Test Matrix**

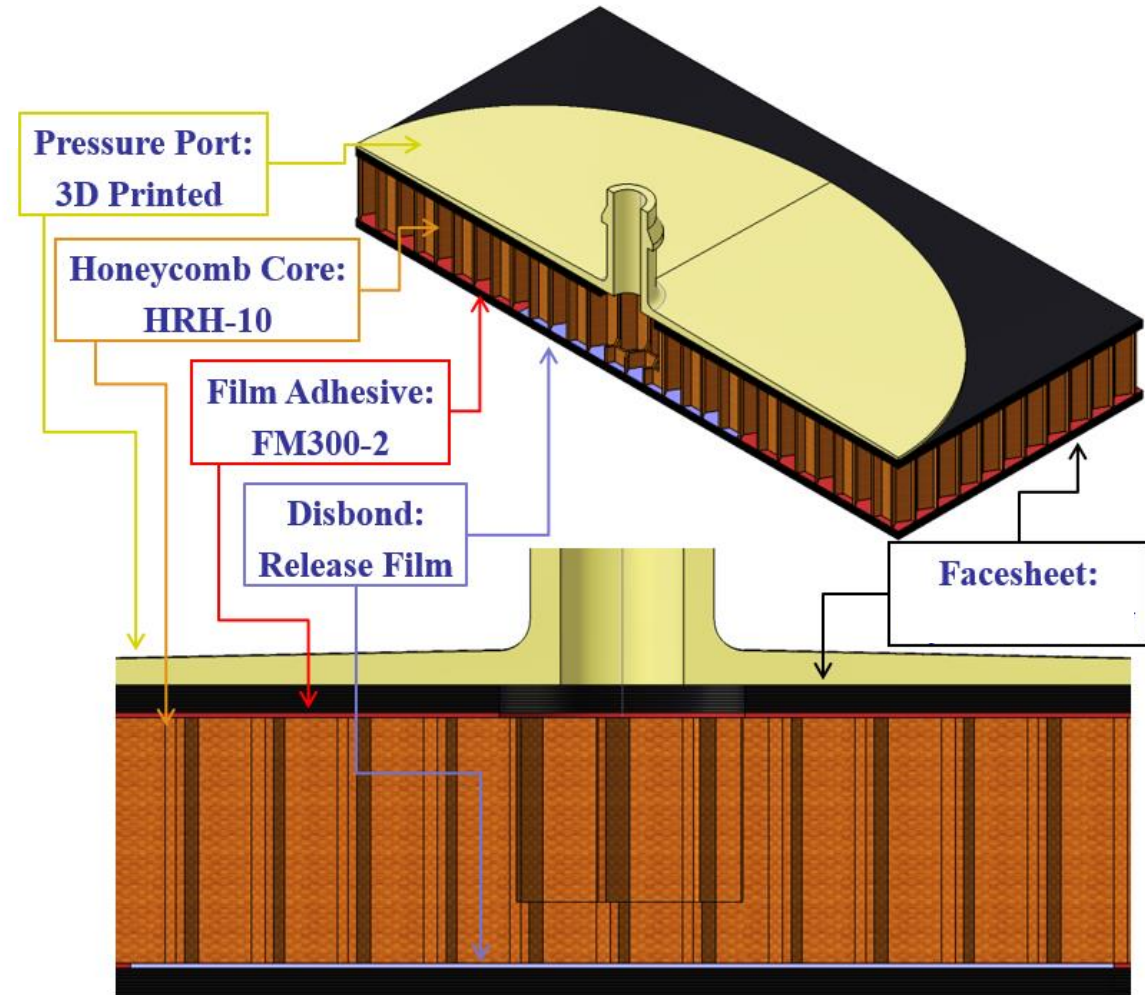
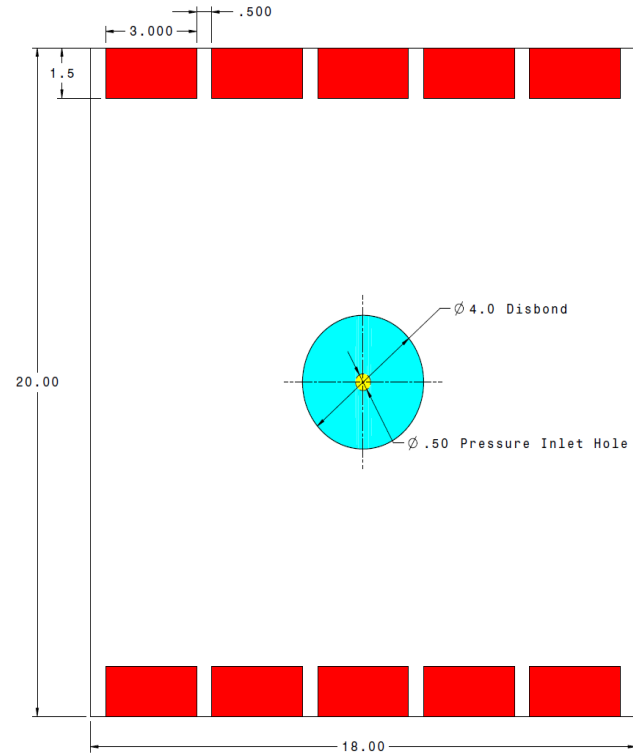
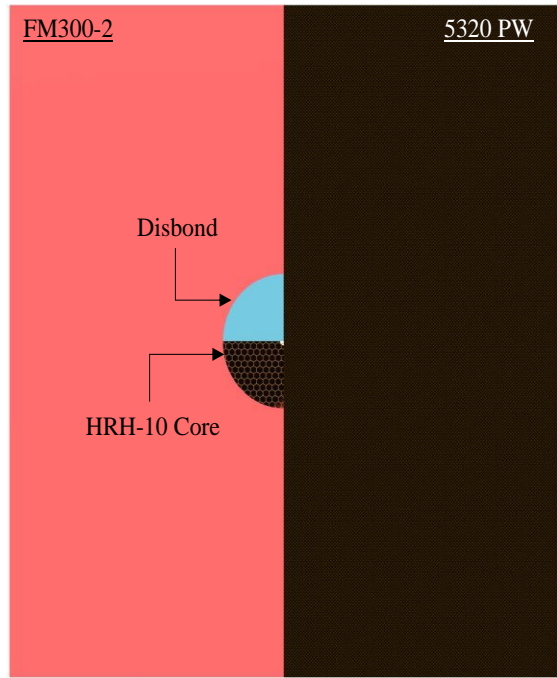
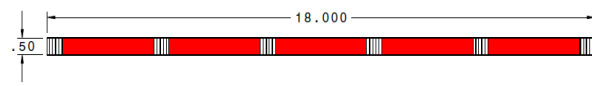
Case	Facesheet Material	Plies	Cell Size (mm)	Core Density (kg/m <sup>3</sup> )	Core Thickness (mm)
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# GAG - Edgewise Compression (EWC) Specimen Configuration





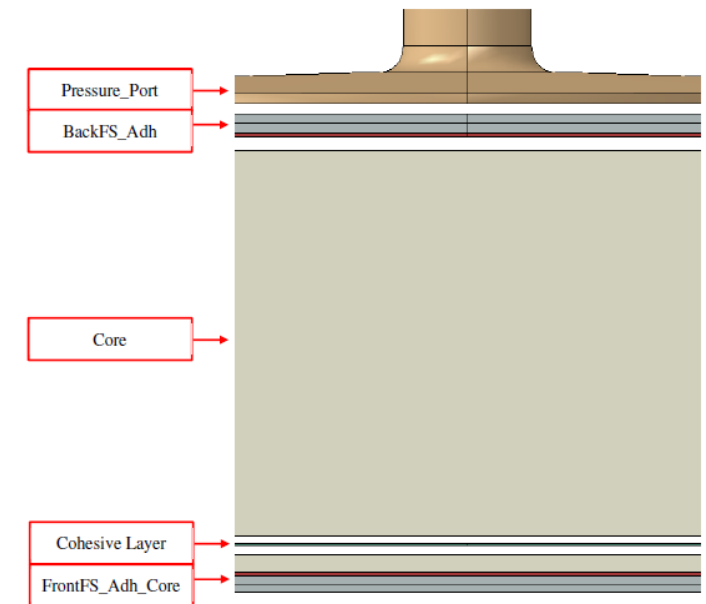
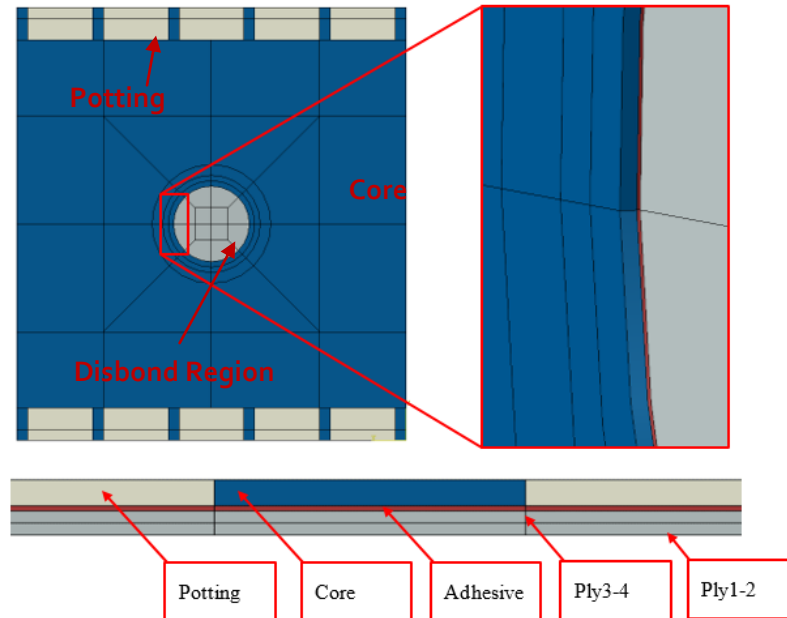
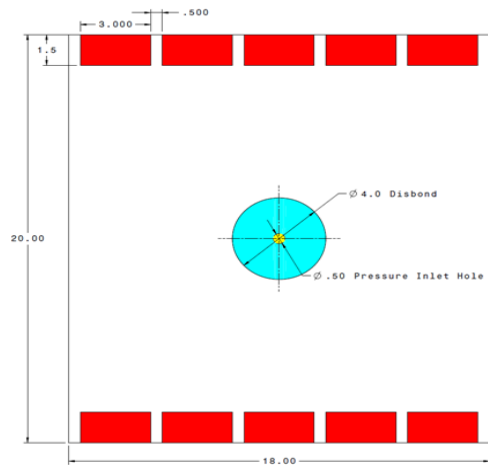
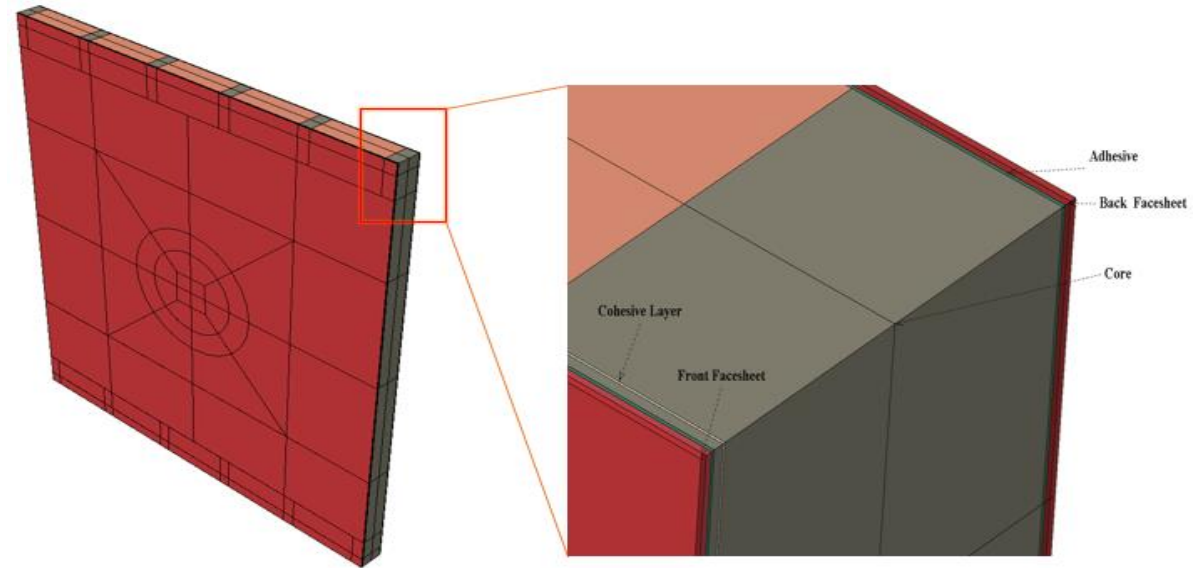
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- SCB Test Configuration
  - Materials & Test Setup (translatable base)
- Foundation Model Approach & Validation
  - Comparison of Foundation, FE & Exp. Results
- Finite Element Model Description of SCB Specimens
  - Cohesive-based modeling approach
- GAG - Edgewise Compression (EWC) Test Configuration
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- **Finite Element Model Description for GAG Specimens**
  - **Modeling approach**
  - **Comparison to test data**
- Summary & Future Work



# FEA – GAG (EWC) FE-Model Description and Approach

- Cohesive based FE analysis – combined static & pressure loading.
- Cohesive parameters from SCB analysis.
  - $G_{1C}$ , Penalty parameters (stiffness,  $K_n$  & strength,  $\tau_n$ )
- Damage modeled in the core (similar to SCB specimens)



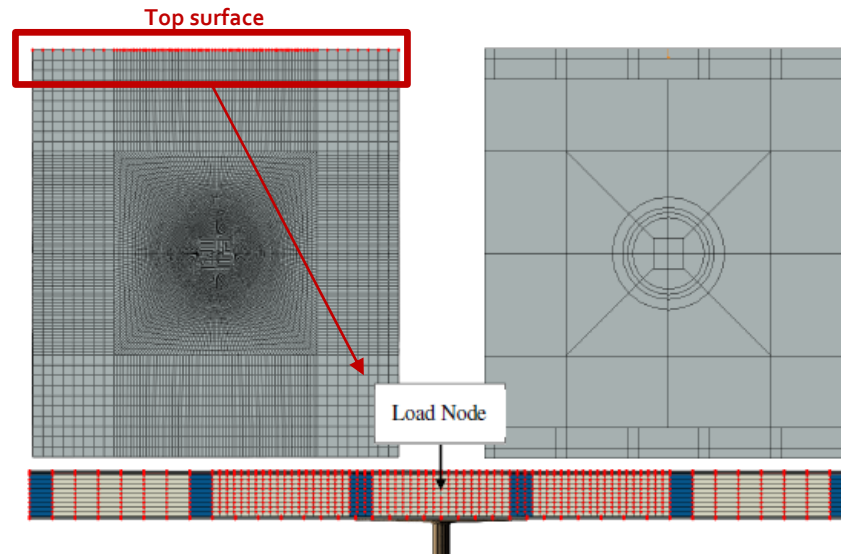
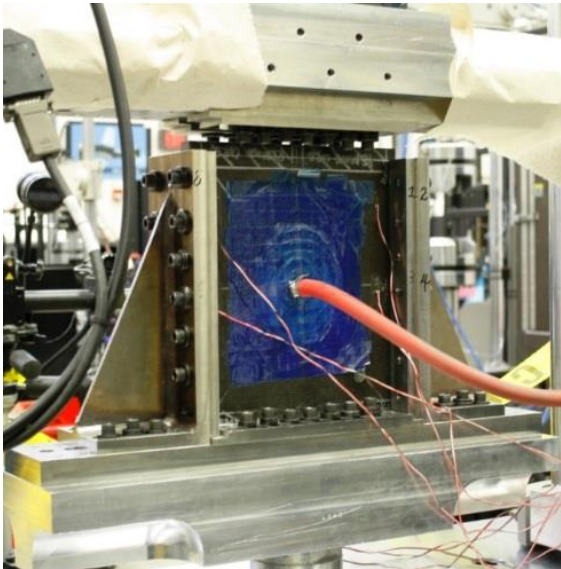




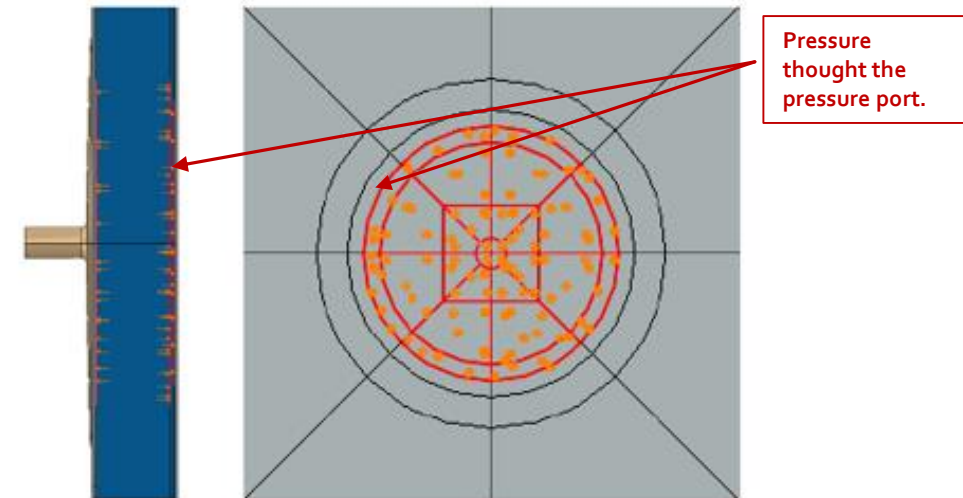
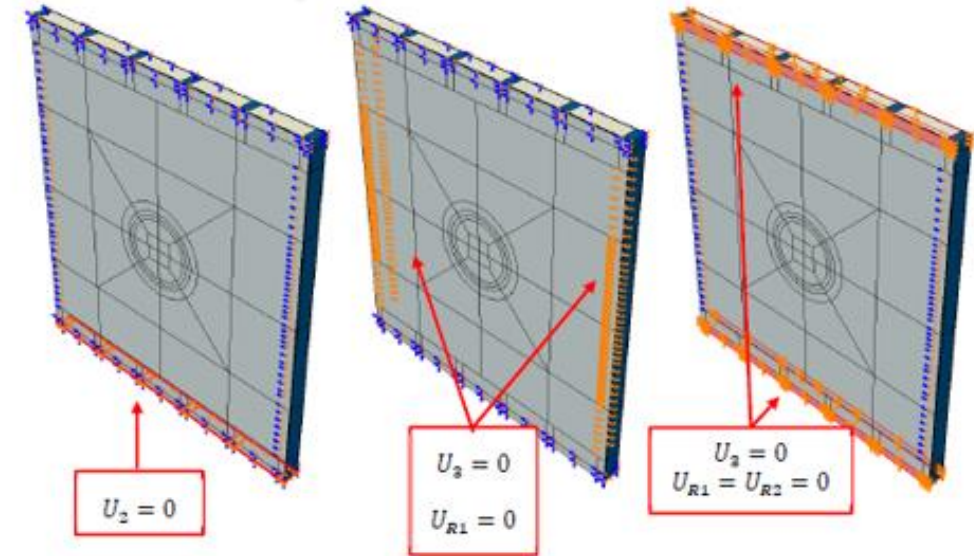
# FEA – GAG (Model Description: Loading and Boundary Conditions)

- Displacement applied at top surface
- Constant pressure (13.1 Psi) applied
- BCs applied on specimen edges to closely replicate the test setup

## Test Setup



## Boundary Conditions and Load Introduction





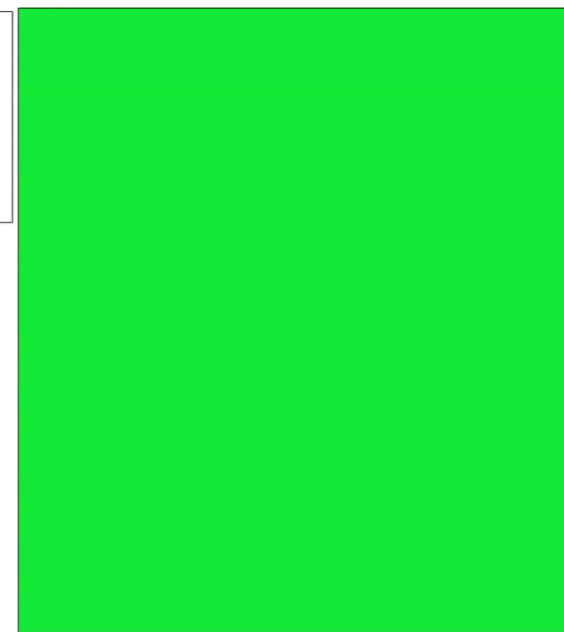
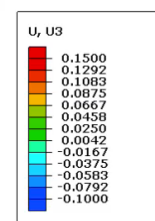
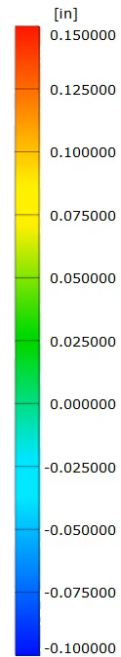
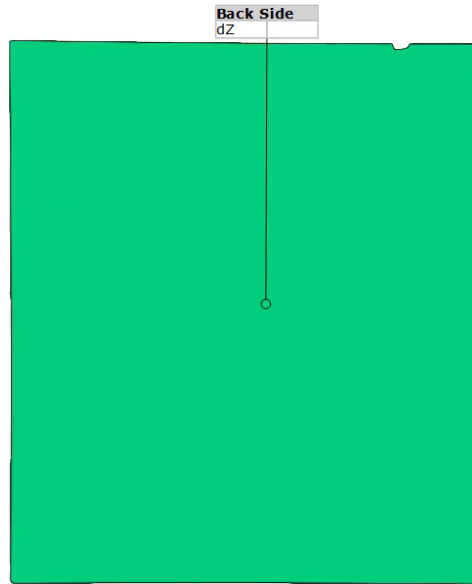


# GAG Test Data Comparison Summary

- Out-of-plane displacement plots (*disp. inches, force in lbf*)
- Crack initiation monitored by deletion of Cohesive elements

8-ply facesheet; 0.5" core

Force  
DIM -34.000 lbf



Step: Comb

Total Time:



# GAG Test Data Comparison Summary

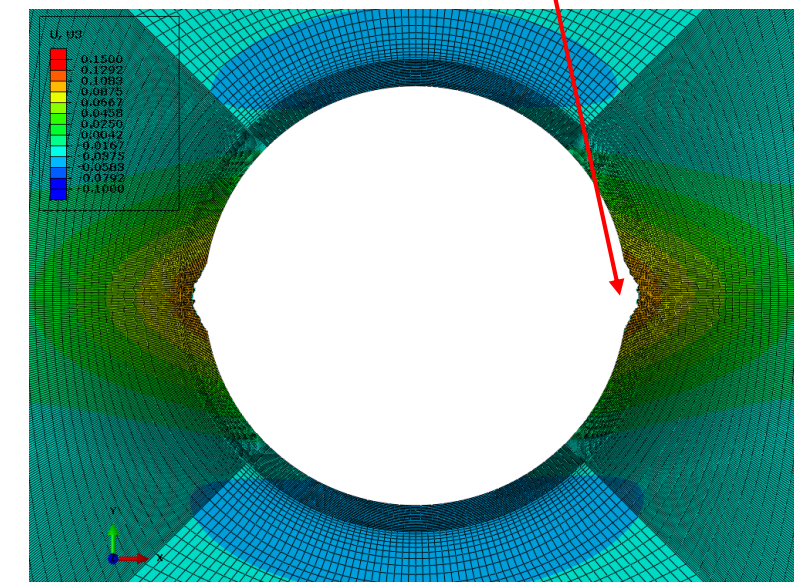
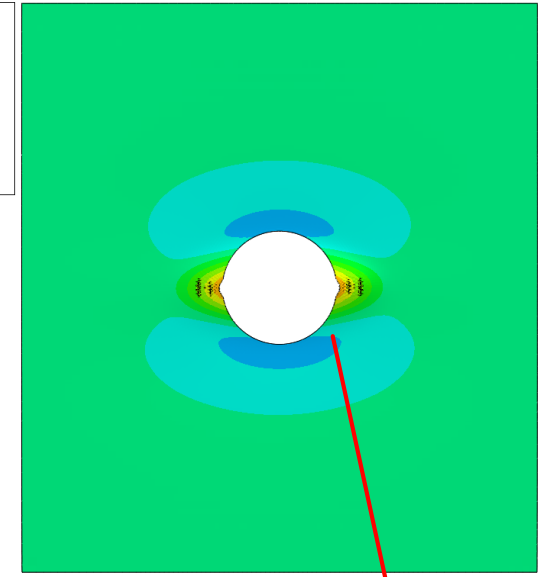
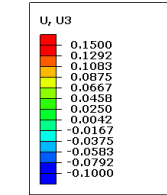
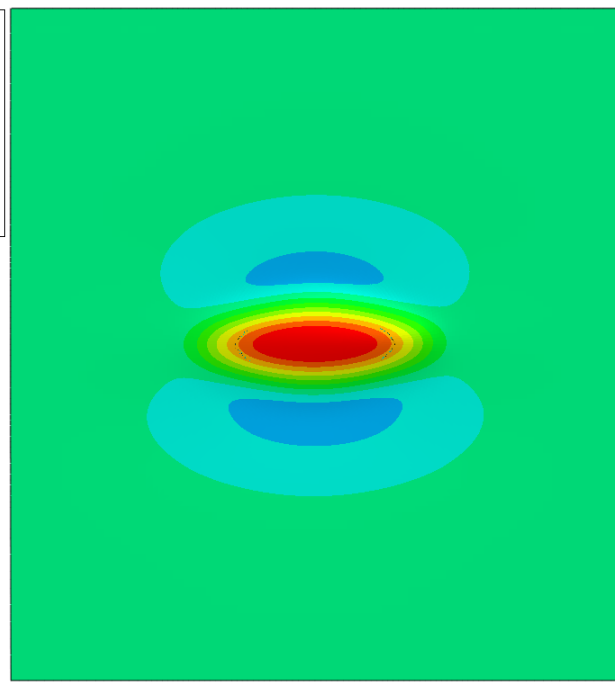
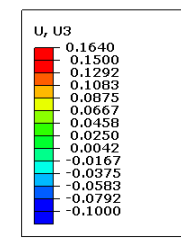
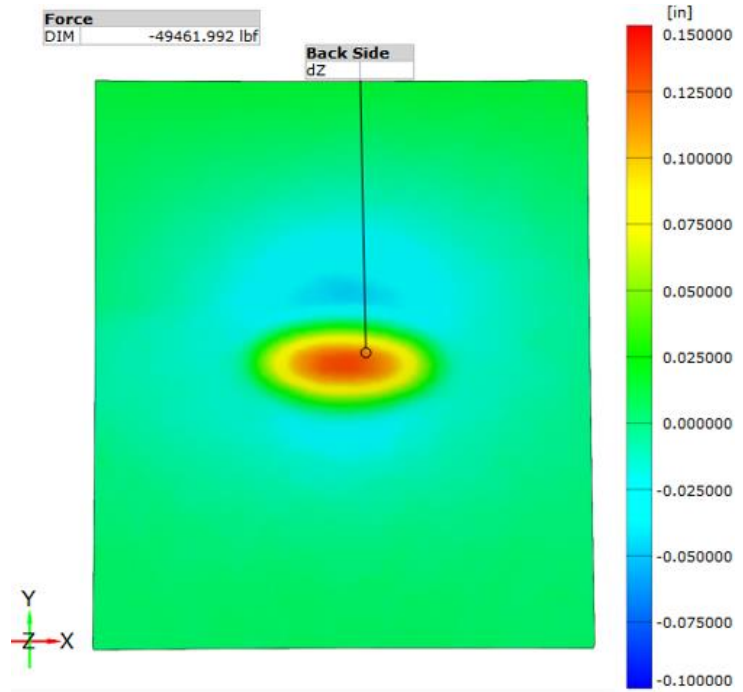
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DIC

8-ply facesheet; 0.5" core

FEA

Cohesive elements





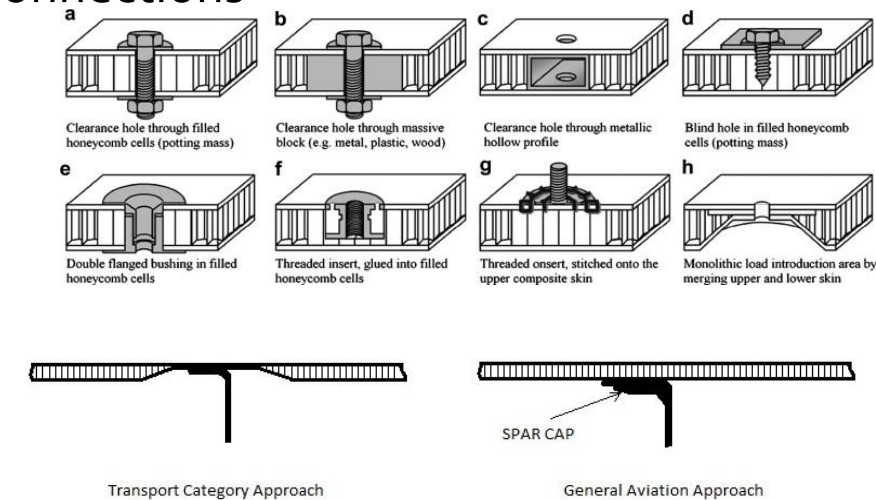
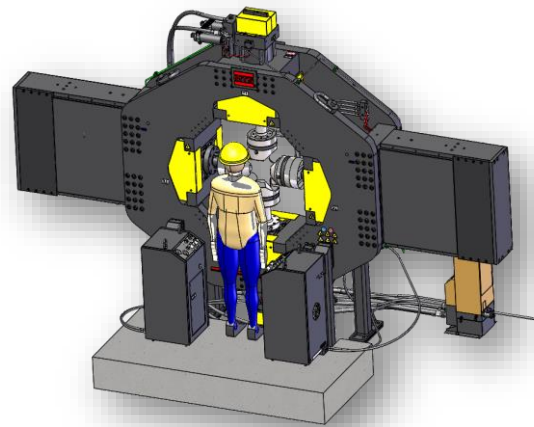
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# Summary & Future Work

- An engineering approach to study debonding presented
  - SCB fracture tests on typical honeycomb core sandwich specimens validated & benchmarked against analytical expressions
  - A test setup capable of applying combined pressure and in-plane loading developed (GAG-cycle)
  - A cohesive zone based FE-model of GAG tests developed
    - FE-model over-predicted for the thicker core; thinner core prediction within the range 3-18%
- The current approach could be expanded to study attachments/connections







# Thank You



## References

1. Tomblin JS, Seneviratne W, Denning S. *Mode I (  $G_{Ic}$  ) Fracture Toughness of Composite Sandwich Structures for Use in Damage Tolerance Design and Analysis: Vol . I Static Testing Including Effects of Fluid Ingression DOT/FAA/TC-16/23*. New Jersey, 2017. DOT/FAA/TC-16/23
2. Tomblin JS, Seneviratne W, Denning S. *Fatigue Damage Growth Rate of Sandwich Structures DOT/FAA/TC-17/6*. New Jersey, 2018
3. Tomblin JS, Seneviratne W, Denning S. *Damage Growth in Sandwich Structures: Supplement to Volume I Testing DOT/FAA/TC-17/7*. New Jersey, 2018.
4. Ratcliffe JG, Reeder JR. Sizing a single cantilever beam specimen for characterizing facesheet-core debonding in sandwich structure. *J Compos Mater* 2011; 45: 2669–2684.
5. Gibson LJ, Ashby MF. *Cellular Solids: Structure and Properties*. Cambridge University Press, 1999
6. El-Sayed, S., & Sridharan, S. (2002). Cohesive layer models for predicting delamination growth and crack kinking in sandwich structures. *International Journal of Fracture*, 117(1), 63-84.



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